

**Table 1. The validated state transitions from a State  $S_i(k)$  to State  $S_j(k+1)$**

	$S_h(k+1)$	$S_c(k+1)$	$S_s(k+1)$	$S_u(k+1)$	$S_p(k+1)$	$S_d(k+1)$	$S_e(k+1)$
$S_h(k)$	$R_{h,h}$	$R_{h,c}$	0	0	0	0	0
$S_c(k)$	$R_{c,h}$	$R_{c,c}$	$R_{c,s}$	0	0	0	0
$S_s(k)$	0	$R_{s,c}$	0	$R_{s,u}$	0	0	0
$S_u(k)$	0	0	$R_{u,s}$	$R_{u,u}$	$R_{u,p}$	0	0
$S_p(k)$	0	0	0	0	0	$R_{p,d}$	0
$S_d(k)$	0	0	0	$R_{d,u}$	0	$R_{d,d}$	$R_{d,e}$
$S_e(k)$	$R_{e,h}$	0	0	0	0	0	0

Equation (1), (2) and (3):

If,

- $/$  denotes the year
- $L$  is the current year
- $m$  is the number of years with historical data available
- $i$  denotes the day of the month
- $j$  is the month of a year. (an exemplary time unit used for simplified demonstration purposes only)

Thus,  $i \in [1, 31]$ ,  $j \in [1, 12]$ ,  $/$  and  $m$  are integers.

$$\bar{x}_j = \frac{1}{m \times n} \sum_{l=L-1}^{L-m} \sum_{i=1}^n x_{l,j,i} \quad (\text{where } i \in [1, 31] \text{ and } j \in [1, 12]) \quad (1)$$

$$s_j = \frac{1}{(m \times n - 1)} \sqrt{\sum_{l=L-1}^{L-m} \sum_{i=1}^n (x_{l,j,i} - \bar{x}_j)^2} \quad (\text{where } i \in [1, 31] \text{ and } j \in [1, 12]) \quad (2)$$

$$C_j = \bar{x}_j + t_{m \times n - 1} s_j \quad (\text{where } i \in [1, 31] \text{ and } j \in [1, 12]) \quad (3)$$

Equation (4), (5) and (6):

$$d_{L,j,i} = \frac{x_{L,j,i} - \bar{x}_j}{\bar{x}_j} \times 100 \quad (L - year, j - month, i - day of month) \quad (4)$$

$$w_{L,j,i} = \sum_{n=0}^{n=6} d_{L,j,i-n} \quad (7 - days cumulated deviation) \quad (5)$$

$$v_{L,j,i} = d_{L,j,i} - d_{L,j,i-1} \quad (change of the daily deviation) \quad (6)$$

Equation (7), (8) and (9):

$$\text{supp}(\alpha(k)) = \{d_{i < L, j, i} ; F(d) \geq (1 - \alpha)\} \quad (7)$$

$$\text{supp}(\beta(k)) = \{w_{i < L, j, i} ; F(w) \geq (1 - \beta)\} \quad (8)$$

$$\text{supp}(\delta(k)) = \{v_{i < L, j, i} ; F(v) \geq (1 - \delta)\} \quad (9)$$

Equation (10), (11), (12), (13), (14) and (15):

$$S_j(k+1) \Leftarrow \{S_i(k) \otimes R_{i,j} \otimes X_i(k), \quad S_i(k) = k_w w_i(k)\} \quad (10)$$

$$X_i(k) \Leftarrow B_{i,m}(\alpha(k), \beta(k), \delta(k)) \otimes \begin{bmatrix} d_{i,m}(k) \\ w_{i,m}(k) \\ v_{i,m}(k) \end{bmatrix} \quad (11)$$

$$Y_i(k) \Leftarrow H_{i,n} \{(\gamma_0(k), \gamma_1(k), \dots, \gamma_n(k)) \otimes \begin{bmatrix} S(k) \\ S(k-1) \\ \dots \\ S(k-n) \end{bmatrix} \otimes G_i(k)\} \quad (12)$$

where

$$X \subset \bigcap_{z=1}^Z \text{supp}(z) \quad (13)$$

$$\text{supp}(z) = \text{supp}(X_{z,1}) \times \text{supp}(X_{z,2}) \times \text{supp}(X_{z,3}) \quad (14)$$

$$Y_i = (Q_{i,h}, T_{i,h}, P_{i,h}) \quad (15)$$